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*Combining parabosons and parafermions in a new graded superalgebra*

When a system of  $m$  parafermions and  $n$  parabosons are combined, there are two choices for the relative commutation relations. One choice (referred to as “of relative parafermion type”) gives rise to the classical orthosymplectic Lie superalgebra  $\mathfrak{osp}(2m+1|2n)$ . For the other choice (of “relative paraboson type”), the underlying algebraic structure is no longer an ordinary Lie superalgebra, but a  $\mathbb{Z}_2 \times \mathbb{Z}_2$ -graded Lie superalgebra, denoted here by  $\mathfrak{ps}\mathfrak{o}(2m+1|2n)$ . Analysing the subalgebra structure of  $\mathfrak{ps}\mathfrak{o}(2m+1|2n)$  allows the investigation of the parastatistics Fock spaces for this new set of  $m+n$  para-operators, as they correspond to lowest weight representations of  $\mathfrak{ps}\mathfrak{o}(2m+1|2n)$ . Our main result is the construction of these Fock spaces, with a complete labeling of the basis vectors and an explicit action of the para-operators on these basis vectors. This is the first example of whole class of representations for a  $\mathbb{Z}_2 \times \mathbb{Z}_2$ -graded Lie superalgebra.