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The higher rank Askey-Wilson algebra and the q-Dirac-Dunkl model

The Askey-Wilson algebra is the q-deformed algebra that underlies the Askey-Wilson polynomials. It is strongly connected with the graded quantum superalgebra $\mathfrak{osp}_q(1|2)$: it arises as its covariance algebra and can be embedded in its threefold tensor product. In this talk I will exploit this connection to generalize the Askey-Wilson algebra to higher rank. This will be done in a slightly different presentation, called the q-Bannai-Ito algebra. I will propose a general extension procedure in the tensor product of n copies of $\mathfrak{osp}_q(1|2)$. The resulting higher rank algebra will have more generators and q-commutation relations and contains the original rank one algebra as its subalgebra. I will present an integrable model as a realization of this algebra, which we will call the \mathbb{Z}_2^n q-Dirac-Dunkl model. We will study the central operator in this model through modules of its null-solutions.

This talk is based on joint work with Hendrik De Bie and Wouter van de Vijver.