
MICHAEL ANTHONY BISHOP, California State University, Fresno

Spectral gaps for the Two-Species Product Vacua and Boundary States models on the d -dimensional lattice

We study the two-species Product Vacua and Boundary States (PVBS) models on the integer lattice \mathbb{Z}^d and prove the existence and non-existence of a spectral gap for all choices of parameters. The PVBS models are spin-1 quantum spin systems which are translation-invariant, frustration-free, and composed of nearest-neighbor non-commuting interactions with both an exclusion property and an interchange interaction between particle species. These models serve as possible representatives of families of automorphically equivalent gapped quantum spin-1 systems on \mathbb{Z}^d . The main result is that the two-species PVBS Hamiltonians have a positive spectral gap when gapped on both of the single-species subspaces and are gapless if gapless on either single-species subspace. The addition of a new particle species does not create any new gapless phases.